NLP1

Sequence Labelling

Wilker Aziz probabll.github.io

ILLC

w.aziz@uva.nl

Week 1

- HC1a: text classification
- HC1b: language modelling

HC2a (today)

• Sequence labelling

In NGram LMs Words are Atomic Symbols

We gave words *categorical treatment*, namely, we treated words as if they were completely unrelated to one another. This led to:

• large tabular cpds

where we store prob of conditional outcomes that are possible

 statistical inneficiency (struggles with data sparsity) linguistically related outcomes do not share statistical evidence

Today we try to overcome this in 2 ways:

- a linguistically-motivated change in the data we model, accompanied by a change in the model and new ideas for *factorisation*
- a change in *parameterisation*

- 1. Word Categories
- 2. Hidden Markov Model
- 3. Evaluation
- 4. Sequence Labelling
- 5. Local Log-Linear Models

Word Categories

Semantic criteria: what does the word refer to?

• nouns often refer to 'people', 'places' or 'things'

Formal criteria: what form does the word have?

- in English, -1y makes an adverb out of an adjective
- in English, -tion makes a noun out of a verb

Distributional criteria: in what contexts can the word occur?

• in English, adjectives precede nouns

Word classes capture aspects of word relatedness.

	Semantically	Formally	Distributionally
Nouns	refer to things,	-ness, -tion,	After determiners,
	concepts	-ity, -ance	possessives
Verbs	refer to actions, states	-ate, -ize	infinitives: to jump, to learn
Adjectives	properties of nouns	-al, -ble	appear before nouns
Adverbs	properties of actions	-ly	next to verbs, beginning of sentence

Word classes enable a form of delexicalised natural language processing in which we can learn about patterns that are common to all words that share a given property (e.g., in English, a pronoun is typically followed by a verb). This depends on what dimensions of 'relatedness' we focus on, and what language we are talking about.

For example, for *Parts-of-Speech* (POS), which mostly capture a word's syntactic function. For English,

- the Brown corpus [Francis and Kucera, 1979] has 87 categories
- the Penn Treebank [Marcus et al., 1993] has 45

Universal POS tags are simplified tags aimed at cross-lingual compatibility (it maps variants of a base class to that base class, e.g., VBD, VBN, VB, VBG, VBP \rightarrow VERB)

Universal Parts-of-Speech [Petrov et al., 2012]

- ADJ (adjectives)
- ADP (prepositions and postpositions)
- ADV (adverbs)
- CONJ (conjunctions)
- DET (determiners and articles)
- NOUN (nouns)
- NUM (numerals)
- PRON (pronouns)
- PRT (particles)
- PUNCT (punctuation marks)
- VERB (verbs)
- X (anything else, such as abbreviations or foreign words)

The/DT grand/JJ jury/NN commented/VBD on/IN a/DT number/NN of/IN other/JJ topics/NNS ./.

There/EX was/VBD still/JJ lemonade/NN in/IN the/DT bottle/NN ./.

Hidden Markov Model

We will prescribe a **joint distribution** over the space of **texts annotated with their POS tags**.

That is, we will be learning to assign probability to sequence pairs of the kind $(w_{1:\ell}, c_{1:\ell})$, where $w_{1:\ell}$ is a *word sequence* and $c_{1:\ell}$ is the corresponding *POS tag sequence*.

Example:
$$(\underbrace{\langle a, \text{ nice, } dog \rangle}_{w_{1:3}}, \underbrace{\langle DT, JJ, NN \rangle}_{c_{1:3}}).$$

- Text analysis: annotating text with POS tags (e.g., input to other tools, such as tools for knowledge extraction)
- Language modelling: address some limitations of NGram LMs (e.g., linguistically related wordforms are treated as such)
- Also, the ideas we develop now will prove useful in many labelling tasks

(e.g., entity recognition, semantic labelling, etc.)

W is a random word. An outcome w is a symbol in a vocabulary W of size V.

C is a random POS tag. An outcome c is a symbol in the tagset C of size K.

 $X = \langle W_1, \dots, W_L \rangle$ is a random word sequence. An outcome $w_{1:\ell}$ is a sequence of ℓ words from \mathcal{W} .

 $Y = \langle C_1, \ldots, C_L \rangle$ is a random tag sequence. An outcome $c_{1:\ell}$ is a sequence of ℓ tags from C.

Design a mechanism to assign probability $P_{XY}(w_{1:\ell}, c_{1:\ell})$ to any outcome $(w_{1:\ell}, c_{1:\ell}) \in W^* \times C^*$.

• factorise $P_{XY}(w_{1:\ell}, c_{1:\ell})$

e.g., chain rule, conditional independencies

• parameterise its elementary factors e.g., tabular Categorical cpds

Estimate the parameters of this mechanism from data (i.e., text annotated with POS tags).

• e.g., use MLE to estimate the free parameters of our parameterisation

Predict a POS tag sequence for a given text.

The outcome assigned largest probability mass is known as the *mode* of the probability distribution.

Predict a POS tag sequence for a given text. For example, via mode-seeking search:

 $\arg \max_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{Y|X}(c_{1:\ell}|w_{1:\ell})$

The outcome assigned largest probability mass is known as the *mode* of the probability distribution.

Predict a POS tag sequence for a given text. For example, via mode-seeking search:

$$\arg \max_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

Assign probability to text that is not annotated with POS tags

The outcome assigned largest probability mass is known as the *mode* of the probability distribution.

Predict a POS tag sequence for a given text. For example, via mode-seeking search:

$$\arg \max_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

Assign probability to text that is *not* annotated with POS tags, via marginalisation:

$$P_X(w_{1:\ell}) = \sum_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{XY}(w_{1:\ell}, c_{1:\ell})$$

The outcome assigned largest probability mass is known as the *mode* of the probability distribution.

Challenge. P_{XY} is a distribution over a countably infinite space of sequence pairs.

Key Idea. Re-express the probability of a sequence pair using the probabilities of the "steps" needed to generate it. Design steps such that they have a simple, countably finite sample space.

Joint observations

the/DET book/NOUN is/VERB on/ADP the/DET table/NOUN ./PUNC

Generative story

BoS

We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

 $the/DET \ book/NOUN \ is/VERB \ on/ADP \ the/DET \ table/NOUN \ ./PUNC$



We pad the tag sequence with a BoS symbol. We pad both sequences with a EoS symbol.

Joint observations

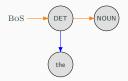
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

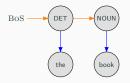
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

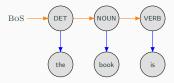
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

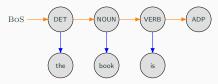
the/DET book/NOUN is/VERB on/ADP the/DET table/NOUN ./PUNC



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

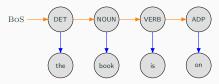
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

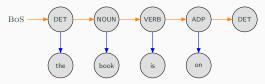
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

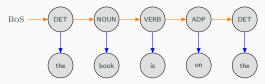
the/DET book/NOUN is/VERB on/ADP the/DET table/NOUN ./PUNC



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

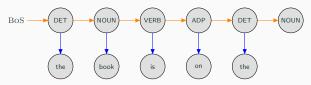
the/DET book/NOUN is/VERB on/ADP the/DET table/NOUN ./PUNC



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

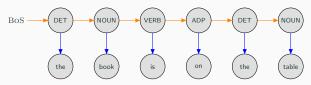
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

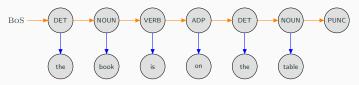
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

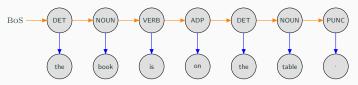
 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Joint observations

 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$



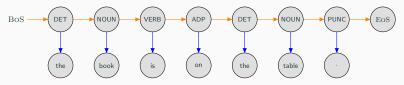
We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Modelling POS-tagged data: illustration

Joint observations

 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$

Generative story



We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Modelling POS-tagged data: illustration

Joint observations

 $the/DET\ book/NOUN\ is/VERB\ on/ADP\ the/DET\ table/NOUN\ ./PUNC$

Generative story



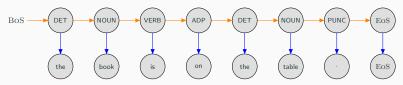
We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Modelling POS-tagged data: illustration

Joint observations

the/DET book/NOUN is/VERB on/ADP the/DET table/NOUN ./PUNC

Generative story



Joint probability

 $\begin{aligned} & P_{C|C_{\text{prev}}}(\text{DET}|\text{BoS})P_{W|C}(\text{the}|\text{DET}) \\ & \times P_{C|C_{\text{prev}}}(\text{NOUN}|\text{DET})P_{W|C}(\text{book}|\text{NOUN}) \\ & \times \dots \\ & \times P_{C|C_{\text{prev}}}(\text{EoS}|\text{PUNC})P_{W|C}(\text{EoS}|\text{EoS}) \end{aligned}$

We pad the tag sequence with a ${\rm BoS}$ symbol. We pad both sequences with a ${\rm EoS}$ symbol.

Conditional independences

- W_i is independent of all but C_i;
- C_i is independent of all but C_{i-1} .

Leading to

$$P_{XY}(w_{1:\ell}, c_{1:\ell}) \stackrel{\text{ind.}}{=} \prod_{i=1}^{\ell} \underbrace{P_{C|C_{\text{prev}}}(c_i|c_{i-1})}_{\text{transition}} \underbrace{P_{W|C}(w_i|c_i)}_{\text{emission}}$$
(1)

Hint. Pad the sequences with a BOS tag (context for the first transition) and EOS tag (for the final transition) and EOS token (for the final emission).

- 1. Start with $X = \langle W_0 = BOS \rangle$, $Y = \langle C_0 = BOS \rangle$ and set i = 1;
- 2. Condition on the previous class c_{i-1} and draw a class c_i with probability $P_{C|C_{prev}}(c_i|c_{i-1})$ extending Y with it;
- Condition on the current class c_i and draw a word w_i with probability P_{W|C}(w_i|c_i) extending X with it;
- 4. If w_i is a special end-of-sequence symbol (EOS), terminate, else increment *i* and repeat from (2).

This specifies a **factorisation** of P_{XY} in terms of elementary factors of the kind $P_{C|C_{prev}}$ and $P_{W|C}$.

Transition distributions. Given a *previous* tag *r*, the transition distribution over (next) tags is Categorical:

$$C|C_{prev} = r \sim \text{Categorical}(\lambda_{1:K}^{(r)})$$

Transition distributions. Given a *previous* tag *r*, the transition distribution over (next) tags is Categorical:

 $C|C_{\text{prev}} = r \sim \text{Categorical}(\lambda_{1:K}^{(r)})$ hence, $P_{C|C_{\text{prev}}}(c|r) = \lambda_c^{(r)}$

Transition distributions. Given a *previous* tag *r*, the transition distribution over (next) tags is Categorical:

$$C|C_{\text{prev}} = r \sim \text{Categorical}(\lambda_{1:K}^{(r)})$$
 hence, $P_{C|C_{\text{prev}}}(c|r) = \lambda_c^{(r)}$

Emission distribution. Given a tag *c*, the emission distribution over words is also Categorical:

 $W|C = c \sim \text{Categorical}(\theta_{1:V}^{(c)})$

Transition distributions. Given a *previous* tag *r*, the transition distribution over (next) tags is Categorical:

$$C|C_{\text{prev}} = r \sim \text{Categorical}(\lambda_{1:K}^{(r)})$$
 hence, $P_{C|C_{\text{prev}}}(c|r) = \lambda_c^{(r)}$

Emission distribution. Given a tag *c*, the emission distribution over words is also Categorical:

$$W|C = c \sim \text{Categorical}(\theta_{1:V}^{(c)})$$
 hence, $P_{W|C}(w|c) = \theta_w^{(c)}$

Probability mass function (pmf).

$$P_{XY}(w_{1:\ell}, c_{1:\ell}) = \prod_{i=1}^{\ell} \underbrace{\lambda_{c_i}^{(c_{i-1})}}_{\text{transition}} \times \underbrace{\theta_{w_i}^{(c_i)}}_{\text{emission}}$$

For *a/DT nice/JJ dog/NN*, we have probability mass:

$\lambda_{\text{DT}}^{(\text{BOS})} \theta_{\text{a}}^{(\text{DT})} \lambda_{\text{JJ}}^{(\text{DT})} \theta_{\text{nice}}^{(\text{JJ})} \lambda_{\text{NN}}^{(\text{JJ})} \theta_{\text{dog}}^{(\text{NN})} \lambda_{\text{EOS}}^{(\text{NN})} \theta_{\text{EOS}}^{(\text{EOS})}$

 Transition. The conditional probability P_{C|Cprev}(c|r) of generating a tag c right after having generated a tag r is

 Transition. The conditional probability P_{C|Cprev}(c|r) of generating a tag c right after having generated a tag r is

$$\lambda_{c}^{(r)} \stackrel{\mathsf{MLE}}{=} \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\sum_{k=1}^{K} \operatorname{count}_{C_{\mathsf{prev}}C}(r,k)} = \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\operatorname{count}_{C_{\mathsf{prev}}}(r)}$$

 Transition. The conditional probability P_{C|Cprev}(c|r) of generating a tag c right after having generated a tag r is

$$\lambda_{c}^{(r)} \stackrel{\mathsf{MLE}}{=} \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\sum_{k=1}^{K} \operatorname{count}_{C_{\mathsf{prev}}C}(r,k)} = \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\operatorname{count}_{C_{\mathsf{prev}}}(r)}$$

 Emission. The conditional probability P_{W|C}(w|c) of generating word w from tag c is

 Transition. The conditional probability P_{C|Cprev}(c|r) of generating a tag c right after having generated a tag r is

$$\lambda_{c}^{(r)} \stackrel{\mathsf{MLE}}{=} \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\sum_{k=1}^{K} \operatorname{count}_{C_{\mathsf{prev}}C}(r,k)} = \frac{\operatorname{count}_{C_{\mathsf{prev}}C}(r,c)}{\operatorname{count}_{C_{\mathsf{prev}}}(r)}$$

 Emission. The conditional probability P_{W|C}(w|c) of generating word w from tag c is

$$\theta_w^{(c)} \stackrel{\mathsf{MLE}}{=} \frac{\operatorname{count}_{CW}(c,w)}{\sum_{o=1}^{V} \operatorname{count}_{CW}(c,o)} = \frac{\operatorname{count}_{CW}(c,w)}{\operatorname{count}_{C}(c)}$$

It's still possible that this model suffers from data sparsity (e.g., unseen transitions or unseen emissions), but much less so than an NGram LM: contextual information is only available through the POS tag of the previous position (only K possible outcomes, instead of V^{N-1} outcomes).

Strong Conditional Independence Assumptions

PLAN as a verb (I read that the government plans to \ldots) or noun (I read the government plans to \ldots)

• older history (read that vs. read the) affects the analysis

HER as possessive determiner (I read *her* book) or personal pronoun (I saw *her* there).

• the (semantics of the) verb (to read vs. to see) affects the analysis

Agreement features cannot always be delexicalised: a cat vs a cats. LIKE as verb (Children like to play outside) or preposition (Children like

their parents need support).

• analysing like requires looking ahead of it

Relax some independencies, e.g.

- trigram transitions: have C_i depend on (C_{i-2}, C_{i-1}) ;
- bigram emissions: have W_i depend on W_{i-1}
- other, e.g., have W_1 depend on C_{i-1} , etc.

These ideas can lead to better models, but tabular representations become larger (and sparser) and they lead to other problems (as we will see next).

Evaluation

Predict a POS tag sequence for novel text. For example via mode-seeking search:

$$\hat{c}_{1:\ell} = rg\max_{1:\ell} P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \ c_{1:\ell} \in \mathcal{C}^\ell$$

Compare predicted $\hat{c}_{1:\ell}$ to human-annotated $c^*_{1:\ell}$ step by step: assess the rate at which the *i*th prediction matches the *i*th target (accuracy). Or, since POS categories are likely imbalanced, compute per-POS F_1 and report macro (or weighted) average.

Let's understand what it means to solve this expression

$$\hat{c}_{1:\ell} = rg\max_{c_{1:\ell} \in \mathcal{C}^\ell} \ P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

the	cute	cat
<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃

Let's understand what it means to solve this expression

$$\hat{c}_{1:\ell} = rg\max_{c_{1:\ell} \in \mathcal{C}^\ell} \ P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

		the	cute	cat
1.	Enumerate <i>all</i>	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
	candidate tag	D	D	D
	sequences	D	D	J
		D	D	Ν
		D	D	V
		D	D	Х
		D	J	D

Let's understand what it means to solve this expression

$$\hat{c}_{1:\ell} = rg\max_{c_{1:\ell} \in \mathcal{C}^\ell} \ P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

		the	cute	cat
1.	Enumerate <i>all</i>	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
		D	D	Х
		D	J	D

Let's understand what it means to solve this expression

$$\hat{c}_{1:\ell} = rg\max_{c_{1:\ell} \in \mathcal{C}^\ell} \ P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

		the	cute	cat
1.	Enumerate all	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
3.	Sort by probability	D	D	Х
	and pick the best	D	J	D

Let's understand what it means to solve this expression

$$\hat{c}_{1:\ell} = rg\max_{c_{1:\ell} \in \mathcal{C}^\ell} \ P_{Y|X}(c_{1:\ell}|w_{1:\ell})$$

. . .

		the	cute	cat
1.	Enumerate all	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
3.	Sort by probability	D	D	Х
	and pick the best	D	J	D

We have K^{ℓ} candidates, enumeration is **intractable**!

Use the HMM to assign probability to observed text $w_{1:\ell}$

$$P_X(w_{1:\ell}) = \sum_{c_{1:\ell} \in \mathcal{C}^\ell} P_{XY}(w_{1:\ell}, c_{1:\ell})$$

Use a heldout dataset and the marginal pmf to assess the perplexity of the model.

Let's understand what it means to solve this expression

 $\sum_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{XY}(w_{1:\ell}, c_{1:\ell})$

the	cute	cat
<i>c</i> ₁	<i>c</i> ₂	C ₃

Let's understand what it means to solve this expression

 $\sum_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{XY}(w_{1:\ell}, c_{1:\ell})$

	the	cute	cat
1. Enumerate <i>all</i>	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
candidate tag	D	D	D
sequences	D	D	J
	D	D	Ν
	D	D	V
	D	D	Х
	D	J	D

Let's understand what it means to solve this expression

 $\sum_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{XY}(w_{1:\ell}, c_{1:\ell})$

		the	cute	cat
1.	Enumerate <i>all</i>	<i>c</i> ₁	<i>c</i> ₂	<i>C</i> 3
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
		D	D	Х
		D	J	D

Let's understand what it means to solve this expression

 $\sum_{c_{1:\ell} \in \mathcal{C}^{\ell}} P_{XY}(w_{1:\ell}, c_{1:\ell})$

		the	cute	cat
1.	Enumerate all	<i>c</i> ₁	<i>c</i> ₂	<i>C</i> 3
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
3.	Sum their	D	D	Х
	probabilities	D	J	D

Let's understand what it means to solve this expression

 $\sum P_{XY}(w_{1:\ell},c_{1:\ell})$ $c_{1\cdot\ell}\in \mathcal{C}^\ell$

. . .

		the	cute	cat
1.	Enumerate <i>all</i>	<i>c</i> ₁	<i>c</i> ₂	<i>c</i> ₃
	candidate tag	D	D	D
	sequences	D	D	J
2.	Assess the probability	D	D	Ν
	of each candidate	D	D	V
3.	Sum their	D	D	Х
	probabilities	D	J	D

We have K^{ℓ} candidates, enumeration is **intractable**!

Enumeration is intractable, but, as it turns out, it's unnecessary.

Because of the conditional independences in the HMM, changing the POS tag of position i can only affect

- one emission probability $(\underline{C_i} \rightarrow w_i)$
- and two transition probabilities $(C_{i-1} \rightarrow \underline{C_i} \text{ and } \underline{C_i} \rightarrow C_{i+1}).$

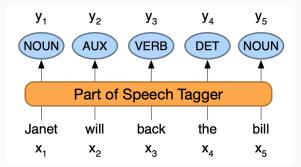
This allows us to solve search and marginalisation incrementally from left to right in time $\mathcal{O}(L \times K^2)$ using the Viterbi or Forward algorithms. Watch the video I prepared for you:

https://youtu.be/rVCd7NrGcSI

Sequence Labelling

POS Tagging

We are **given** the text and we do not care to assign probability to it.



Our goal is to develop a system that can POS tag the input sequence.

Figure from Ch17 https://web.stanford.edu/~jurafsky/slp3/17.pdf 29

NER is a labelling task from a semantic perspective, where we recognise proper nouns that refer to a certain type of entity.

Citing high fuel prices, [ORG United Airlines] said [TIME Friday] it has increased fares by [MONEY \$6] per round trip on flights to some cities also served by lower-cost carriers. [ORG American Airlines], a unit of [ORG AMR Corp.], immediately matched the move, spokesman [PER Tim Wagner] said. [ORG United], a unit of [ORG UAL Corp.], said the increase took effect [TIME Thursday] and applies to most routes where it competes against discount carriers, such as [LOC Chicago] to [LOC Dallas] and [LOC Denver] to [LOC San Francisco].

The text (in black) is **given** and we do not care to assign probability to it. Our goal is to develop a system that can detect and categorise mentions to named entities (i.e., the blue spans)

Figure from Ch17 https://web.stanford.edu/~jurafsky/slp3/17.pdf

Chunking as Labelling

We can see NER as sequence labelling by labelling tokens as inside or outside a span of text that refers to a named-entity.

Words	IO Label	BIO Label	BIOES Label	
Jane	I-PER	B-PER	B-PER	
Villanueva	I-PER	I-PER	E-PER	
of	0	0	0	
United	I-ORG	B-ORG	B-ORG	
Airlines	I-ORG	I-ORG	I-ORG	
Holding	I-ORG	I-ORG	E-ORG	
discussed	0	0	0	
the	0	0	0	
Chicago	I-LOC	B-LOC	S-LOC	
route	0	0	0	
	0	0	0	
Figure 17.7 NER as a sequence model, showing IO, BIO, and BIOES taggings.				

These annotation schemes fit right into the sequence labelling framework we developed for POS tagging.

Because HMMs need to generate text, they power sequence labellers that make fairly limited use of linguistic context in $w_{1:\ell}$. Having C_i interact with words other than W_i would make key quantities in the HMM **very** hard to compute (e.g., marginal and mode probabilities). It would also make the tabular CPDs rather

sparse.

Unseen words and phrases (e.g., proper names and acronyms, inflected verbs, phrasal verbs) are actually quite frequent.

In many cases, their likely interpretation (e.g., syntactic or semantic function) are identifiable from fine-grained features: capitalisation (in English), prefixes and suffixes (e.g., 'un-' or '-ed'), knowing the words surrounding a certain position (e.g., a window of 5 words), etc.

Local Log-Linear Models

Sequence labelling tasks map from a token sequence to the tag sequence that's assigned highest probability under the model

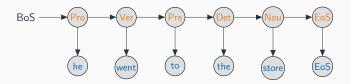
$$\hat{c}_{1:\ell} = rg\max_{1:\ell} P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \ c_{1:\ell} \in \mathcal{C}^\ell$$

In an HMM, we obtain this conditional by *inferring* it from a joint distribution (which we design, i.e., factorise and parameterise).

What if, instead, we attempted to factorise and parameterise this conditional *directly*?

Conditional modelling

The HMM is a *generative model* of labelled text.



We may choose to regard the text as a predictor, and *model the conditional distribution of tag sequences*.



First Idea: 0-order model

Let's start even simpler and make a 0-order Markov assumption: $C_i \perp C_{j \neq i} | X = x, I = i.$

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \stackrel{\text{ind.}}{=} \prod_{i=1}^{\ell} P_{C|XI}(c_i|w_{1:\ell}, i)$$

$$(4)$$

$$\stackrel{\text{Pro}}{\longrightarrow} \bigvee_{\text{went}} \bigvee_{\text{to}} \bigvee_{\text{to}} \bigvee_{\text{the}} \bigvee_{\text{store}} \bigvee_{\text{EoS}}$$

 $C_i \perp C_{j \neq i} | X = x, I = i$ is pronounced: given x and that we want to tag the *i*th word, the distribution of the *i*th tag C_i is independent of the rest of the tag sequence.

First Idea: 0-order model

Let's start even simpler and make a 0-order Markov assumption: $C_i \perp C_{j \neq i} | X = x, I = i.$

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \stackrel{\text{ind.}}{=} \prod_{i=1}^{\ell} P_{C|XI}(c_i|w_{1:\ell}, i)$$

$$(4)$$

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \stackrel{\text{ind.}}{=} \prod_{i=1}^{\ell} P_{C|XI}(c_i|w_{1:\ell}, i)$$

To make this happen, we will need to rethink parameterisation!

 $C_i \perp C_{j \neq i} | X = x, I = i$ is pronounced: given x and that we want to tag the *i*th word, the distribution of the *i*th tag C_i is independent of the rest of the tag sequence.

Rethinking Parameterisation

In the 0-order conditional model, the cpd of any one tag depends on the entire text $w_{1:\ell}$, for each position $i \in [\ell]$.

$$C \mid \underbrace{X = w_{1:\ell}, I = i}_{\text{conditioning context}} \sim \text{Categorical}(\bigsqcup_{1, \dots, \bigsqcup_{K}})$$

Since the conditioning context is a high-dimensional, variable-length outcome, we cannot give this cpd tabular treatment (i.e., store conditional probs for every $(w_{1:\ell}, i)$).

Instead we can **learn to predict conditional probs** from a *D*-dimensional representation of the conditioning context.

Note how this parallels the design of a text classifier: in a given textual context we want to predict a distribution over K labels.

Let $\phi(w_{1:\ell}, i) \in \mathbb{R}^D$ be a feature vector representing ('describing') the *i*th position of $w_{1:\ell}$.

Examples:

• $\phi(\langle \text{he, went, } \underline{\text{to}}, \text{ the, store} \rangle, 3)$ is a vector **u** such that $u_{\text{id}(\text{word:to})} = 1$, $u_{\text{id}(\text{before:went})} = 1$, $u_{\text{id}(\text{after:the})} = 1$, $u_{\text{id}(\text{position})} = \frac{3}{5}$, and other coordinates of **u** are 0;

Let $\phi(w_{1:\ell}, i) \in \mathbb{R}^D$ be a feature vector representing ('describing') the *i*th position of $w_{1:\ell}$.

Examples:

- $\phi(\langle \text{he, went, } \underline{\text{to}}, \text{ the, store} \rangle, 3)$ is a vector **u** such that $u_{\text{id}(\text{word:to})} = 1$, $u_{\text{id}(\text{before:went})} = 1$, $u_{\text{id}(\text{after:the})} = 1$, $u_{\text{id}(\text{position})} = \frac{3}{5}$, and other coordinates of **u** are 0;
- $\phi(\langle \text{he, went, to, the, } \underline{\text{store}} \rangle, 5)$ is a vector **v** such that $v_{id(\text{word:store})} = 1$, $v_{id(\text{before:the})} = 1$, $v_{id(\text{after:EOS})} = 1$, $v_{id(\text{position})} = \frac{5}{5}$, and other coordinates of **v** are 0;

We map any given conditioning context $(w_{1:\ell}, i)$ to a K-dimensional probability vector by

- 1. mapping it to the real coordinate space;
- 2. linearly mapping the result to K scores;
- 3. projecting the result to the probability simplex:

$$\mathbf{f}(w_{1:\ell}, i; \theta) = \operatorname{softmax}(\overbrace{\mathbf{W}}_{\substack{\phi(w_{1:\ell}, i) \\ \text{step 1}}}^{\text{step 2}} + \mathbf{b})$$

with $\boldsymbol{\theta} = \{ \mathbf{W} \in \mathbb{R}^{K \times D}, \mathbf{b} \in \mathbb{R}^{K} \}.$

Here are templates for the coordinates of a feature function $\phi(w_{1:\ell}, i)$: word: w_i , before: w_{i-1} , after: w_{i+1} , all binary-valued. If we know a total of V words, what is the dimensionality D of this feature space?

What if we add the templates before $2: w_{i-2}$ and after $2: w_{i+2}$?

And what if we add the templates wordpref:prefix(w_i), wordsuff:suffix(w_i) and wordstem:stem(w_i)? Assume we know Rprefixes, S suffixes, and a number $V' \propto V$ of stems.

For example, prefix(unwanted) = un, stem(unwanted) = want, suffix(unwanted) = ed.

Pmf

For $i \in [\ell]$, here's our model

$$C \mid \underbrace{X = w_{1:\ell}, l = i}_{\text{conditioning context}} \sim \text{Categorical}(\underbrace{f(w_{1:\ell}, i; \theta)}_{\text{predicted probs}})$$

Here's the pmf

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) = \prod_{i=1}^{\ell} P_{C|XI}(c_i|w_{1:\ell}, i)$$

=
$$\prod_{i=1}^{\ell} [\mathbf{f}(w_{1:\ell}, i; \theta)]_{c_i}$$
(5)

The notation $[\mathbf{v}]_i$ is equivalent to v_i , it's easier to read when the vector argument is the output of a function with multiple arguments.

Pmf

For $i \in [\ell]$, here's our model

$$C \mid \underbrace{X = w_{1:\ell}, l = i}_{\text{conditioning context}} \sim \text{Categorical}(\underbrace{f(w_{1:\ell}, i; \theta)}_{\text{predicted probs}})$$

Here's the pmf

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) = \prod_{i=1}^{\ell} P_{C|XI}(c_i|w_{1:\ell}, i)$$

=
$$\prod_{i=1}^{\ell} [\mathbf{f}(w_{1:\ell}, i; \theta)]_{c_i}$$
(5)

Note how this amounts to designing 1 'text classifier'-type thing and re-using it for each and every step of the sequence.

The notation $[\mathbf{v}]_i$ is equivalent to v_i , it's easier to read when the vector argument is the output of a function with multiple arguments.

About the 0-order model we designed.

Claim 1: it cannot be used as a language model.

Claim 2: finding the best tag sequence for a given text $w_{1:\ell}$ can be done by solving a sequence of ℓ independent classifications.

Accept or reject the claims, justifying your decision in each case.

Likelihood Function

Just like before, we do MLE. Unlike before, this time we will not have an exact, closed-form expression.

We have a training corpus $\mathcal{D} = \{(x_1, y_1), \dots, (x_N, y_N)\}$ of N data points, the *n*th of which is a labelled sequence of length ℓ_n .

We assess the log-likelihood of ${m heta}$ given ${\cal D}$

$$\mathcal{C}_{\mathcal{D}}(\boldsymbol{\theta}) = \sum_{n=1}^{N} \log P_{Y|X}(y_n|x_n)$$

$$= \sum_{n=1}^{N} \sum_{i=1}^{\ell_n} \log \underbrace{P_{C|XI}(y_{n,i}|x_n, i)}_{=[\mathbf{f}(x_n, i; \boldsymbol{\theta})]_{c_{n,i}}}$$
(6)

The technical term from statistics is *likelihood of model parameter given* observed data, in ML and applied ML, esp in recent years, $\mathcal{L}_{\mathcal{D}}(\theta)$ is often referred to as 'likelihood of data'.

We search for the parameter value that optimises the log-likelihood function:

$$\theta^{\mathsf{MLE}} = rg\max_{\theta} \mathcal{L}_{\mathcal{D}}(\theta)$$
 (7)

There's no closed-form solution to this optimisation problem (for our log-linear model), but we can approximately solve it via an iterative gradient-based optimisation

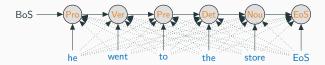
$$\boldsymbol{\theta}' = \boldsymbol{\theta} + \gamma \boldsymbol{\nabla}_{\boldsymbol{\theta}} \mathcal{L}_{\mathcal{D}}(\boldsymbol{\theta}) \tag{8}$$

We typically use autodiff [Baydin et al., 2018] and a stochastic optimiser.

More Dependencies: 1-order model

We could make a 1-order Markov assumption:

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \triangleq \prod_{i=1}^{\ell} P_{C|XIC_{\text{prev}}}(c_i|w_{1:\ell}, i, c_{i-1})$$
(9)

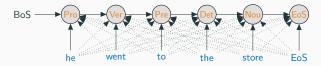


 $C_i \perp C_{j \notin \{i-1,i\}} | X = x, I = i, C_{prev} = r$: given x, that we want to tag the *i*th word, and that the previous word received tag $C_{prev} = r$, the distribution of the *i*th tag C_i is independent of all but the previous tag in the tag sequence.

More Dependencies: 1-order model

We could make a 1-order Markov assumption:

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \triangleq \prod_{i=1}^{\ell} P_{C|XIC_{\text{prev}}}(c_i|w_{1:\ell}, i, c_{i-1})$$
(9)



A feature function for this has access to the *previous class*: e.g., $\phi(\langle \text{he, went, } \underline{\text{to}}, \text{ the, store} \rangle, 3, \text{Verb})$ is a vector **u** such that $u_{\text{id}(\text{word:to})} = 1$, $u_{\text{id}(\text{before:went})} = 1$, $u_{\text{id}(\text{after:the})} = 1$, $u_{\text{id}(\text{position})} = \frac{3}{5}$, $u_{\text{id}(\text{prevtag:Verb})} = 1$ and other coordinates are 0

 $C_i \perp C_{j \notin \{i-1,i\}} | X = x, I = i, C_{prev} = r$: given x, that we want to tag the *i*th word, and that the previous word received tag $C_{prev} = r$, the distribution of the *i*th tag C_i is independent of all but the previous tag in the tag sequence.

Claim 1. Compared to the example feature function for the 0-order model, the example feature function for the 1-order model has K new coordinates.

Claim 2. Finding the best tag sequence for the 1-order model can be done as follows: start with $\hat{c}_0 = BOS$, iteratively for each *i* from 1 to ℓ , solve:

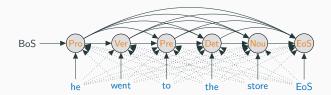
$$\hat{c}_i = \underset{k \in [K]}{\arg \max} P_{C|XI}(k|w_{1:\ell}, i, \hat{c}_{i-1})$$

Accept or reject the claims, justifying your decision in each case.

Conditional Chain Rule

We could use chain rule, conditioned on the word sequence

$$P_{Y|X}(c_{1:\ell}|w_{1:\ell}) \triangleq \prod_{i=1}^{\ell} P_{C|XH}(c_i|w_{1:\ell}, c_{(10)$$



For now, a powerful feature function for this is not trivial to design. That's because to describe the complex dependencies in the history using *indicators*, we increase the dimensionality of the feature space exponentially with length of history.

Overview

Log-linear models can achieve a lot!

- We can use more context, word internal features, etc.
- They are more statistically efficient than tabular cpds: the size of the model does not depend on how many condition-outcome pairs are possible.
- They have been applied to POS tagging, NER, semantic role labelling, etc.

But they are tricky to design

- Good feature functions require enough intuitions about what's likely useful for a task.
- Interesting feature spaces are typically very large.

Summary

- HMMs combine generation and classification, they can be used as taggers or LMs.
- HMMs make strong factorisation assumptions and have are parameterised inefficiently (tabular cpds).
- Log-linear models are a good alternative parameterisation of Categorical cpds.
- Local log-linear models can power direct modelling of complex conditional distributions.
- These ideas power various sequence labelling tasks.

We can extend these in two ways: global modelling (not covered in this course, look for CRFs), and fewer Markov assumptions (with neural parameterisation).

Self-study

- Exercises throughout slides (solutions at the end of slides)
- Watch the video on Viterbi/Forward
- Watch the videos on logistic CPDs: theory, example, and code.

Solutions

Feature Spaces

Here are templates for the coordinates of a feature function $\phi(w_{1:\ell}, i)$: word: w_i , before: w_{i-1} , after: w_{i+1} , all binary-valued. If we know a total of V words, what is the dimensionality D of this feature space? The feature space has to accommodate every possible instantiation of those templates, there are V ways to instantiate each of the 3 templates, hence $D = 3 \times V$.

What if we add the templates before2: w_{i-2} and after2: w_{i+2} ? That would increment D with $2 \times V$ features, since each of these templates can be instantiated in V possible ways.

And what if we add the templates wordpref:prefix(w_i), wordsuff:suffix(w_i) and wordstem:stem(w_i)? Assume we know R prefixes, S suffixes, and a number $V' \propto V$ of stems. The are R ways to instantiate the wordpref template, S ways to instantiate the wordsuff template, and a number $V' \propto V$ ways to instantiate the template wordstem, hence we would increment D by R + S + V'. About the 0-order model we designed.

Claim 1: it cannot be used as a language model.

This is true because the model is not inferred from a joint distribution over the space of labelled text, instead, it is a probability distribution directly specified over the space of tag sequences.

Claim 2: finding the best tag sequence for a given text $w_{1:\ell}$ can be done by solving a sequence of ℓ independent classifications.

This is true because the definition of the Categorical parameter $f(W\phi(w_{1:\ell}, i) + \mathbf{b})$ is such that for any position *i* we would like to classify, it only has access to the text $w_{1:\ell}$ itself. In other words, for each and every step, there are no dependencies on other tags, and hence the tagging of each position is independent of the tagging of any other position.

About 1st-order model

Claim 1. Compared to the example feature function for the 0-order model, the example feature function for the 1-order model has K new coordinates.

This is true because the new feature function has a template prevtag: c_{i-1} for the previous tag, which can be instantiated in K possible ways.

Claim 2. Finding the best tag sequence for the 1-order model can be done as follows: start with $\hat{c}_0 = BOS$, iteratively for each *i* from 1 to ℓ , solve:

$$\hat{c}_i = \underset{k \in [K]}{\operatorname{arg\,max}} P_{C|XI}(k|w_{1:\ell}, i, \hat{c}_{i-1})$$

This is false because now each tagging decision depends on the tagging decision done previously. It is possible that a decision that's locally optimal for step i = 2 is not globally optimal a few steps later. *Extra information for you:* To solve this correctly, we need dynamic programming. As the *unobserved* variables of this problem (the tags in the tag sequence) depend on one another in the same way as they would in the standard HMM (i.e., in a 1st-order linear chain), we can actually use a version of the Viterbi algorithm for this.

References

- Atilim Gunes Baydin, Barak A. Pearlmutter, Alexey Andreyevich Radul, and Jeffrey Mark Siskind. Automatic differentiation in machine learning: a survey. *Journal of Machine Learning Research*, 18(153):1–43, 2018. URL http://jmlr.org/papers/v18/17-468.html.
- W Nelson Francis and Henry Kucera. Brown corpus manual. Letters to the Editor, 5(2):7, 1979.
- Mitchell P. Marcus, Beatrice Santorini, and Mary Ann Marcinkiewicz. Building a large annotated corpus of English: The Penn Treebank. *Computational Linguistics*, 19(2):313–330, 1993. URL https://aclanthology.org/J93-2004.

Slav Petrov, Dipanjan Das, and Ryan McDonald. A universal part-of-speech tagset. In Nicoletta Calzolari, Khalid Choukri, Thierry Declerck, Mehmet Uğur Doğan, Bente Maegaard, Joseph Mariani, Asuncion Moreno, Jan Odijk, and Stelios Piperidis, editors, Proceedings of the Eighth International Conference on Language Resources and Evaluation (LREC'12), pages 2089–2096, Istanbul, Turkey, May 2012. European Language Resources Association (ELRA). URL http://www.lrec-conf.org/proceedings/lrec2012/pdf/ 274_Paper.pdf.