Natural Language Processing 1 Lecture 5: Lexical semantics and word embeddings

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Natural Language Processing 1

Introduction to lexical semantics

Outline.

Introduction to lexical semantics

Distributional semantics

Semantics with dense vectors

Semantics

Compositional semantics:

- studies how meanings of phrases are constructed out of the meaning of individual words
- principle of compositionality: meaning of each whole phrase derivable from meaning of its parts
- sentence structure conveys some meaning: obtained by syntactic representation

Lexical semantics:

 studies how the meanings of individual words can be represented and induced

What is lexical meaning?

- recent results in psychology and cognitive neuroscience give us some clues
- but we don't have the whole picture yet
- different representations proposed, e.g.
 - formal semantic representations based on logic,
 - or taxonomies relating words to each other,
 - or distributional representations in statistical NLP
- but none of the representations gives us a complete account of lexical meaning

How to approach lexical meaning?

- Formal semantics: set-theoretic approach e.g., cat': the set of all cats; bird': the set of all birds.
- meaning postulates, e.g.

 $\forall x [bachelor'(x) \rightarrow man'(x) \land unmarried'(x)]$

- Limitations, e.g. is the Pope a bachelor?
- Defining concepts through enumeration of all of their features in practice is highly problematic
- How would you define e.g. chair, tomato, thought, democracy? impossible for most concepts
- Prototype theory offers an alternative to set-theoretic approaches

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Prototype theory

- introduced the notion of graded semantic categories
- no clear boundaries; no requirement that a property be shared by all members
- certain members of a category are more central or prototypical (i.e. instantiate the prototype)

furniture: chair is more prototypical than stool

 Categories form around prototypes; new members added on basis of resemblance to prototype

Eleanor Rosch 1975. *Cognitive Representation of Semantic Categories* (J Experimental Psychology)

Semantic relations

Hyponymy: IS-A

dog is a hyponym of *animal animal* is a hypernym of *dog*

- hyponymy relationships form a taxonomy
- works best for concrete nouns

Other semantic relations

Meronomy: PART-OF e.g., *arm* is a meronym of *body*, *steering wheel* is a meronym of *car*

Synonymy e.g., aubergine/eggplant.

Antonymy e.g., big/little

Also:

Near-synonymy/similarity e.g., *exciting/thrilling* e.g., *slim/slender/thin/skinny*

WordNet: a large-scale lexical resource linking words by their semantic relations.

Polysemy and word senses

The children **ran** to the store If you see this man, **run**! Service **runs** all the way to Cranbury She is **running** a relief operation in Sudan the story or argument **runs** as follows Does this old car still **run** well? Interest rates **run** from 5 to 10 percent Who's **running** for treasurer this year? They **ran** the tapes over and over again These dresses **run** small

Polysemy

- homonymy: unrelated word senses. bank (raised land) vs bank (financial institution)
- bank (financial institution) vs bank (in a casino): related but distinct senses.
- regular polysemy and sense extension
 - metaphorical senses, e.g. *swallow* [food], *swallow* [information], *swallow* [anger]
 - metonymy, e.g. he played *Bach*; he drank his *glass*.
 - zero-derivation, e.g. tango (N) vs tango (V)

No clearcut distinctions between different senses, in many cases.

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Distributional semantics

Outline.

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Distributional semantics

Semantics with dense vectors

Distributional hypothesis

You shall know a word by the company it keeps (Firth) The meaning of a word is defined by the way it is used (Wittgenstein).

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Distributional semantics

Scrumpy



Distributional hypothesis

This leads to the distributional hypothesis about word meaning:

- the context surrounding a given word provides information about its meaning;
- words are similar if they share similar linguistic contexts;
- semantic similarity \approx distributional similarity.

The general intuition

- Distributions are vectors in a multidimensional semantic space.
- The semantic space has dimensions which correspond to possible contexts features.
- For our purposes, a distribution can be seen as a point in that space (the vector being defined with respect to the origin of that space).
- scrumpy [...pub 0.8, drink 0.7, strong 0.4, joke 0.2, mansion 0.02, zebra 0.1...]

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Distributional semantics

Vectors



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The notion of context

1 Word windows (unfiltered): *n* words on either side of the lexical item.

Example: n=2 (5 words window):

| The prime **minister** acknowledged the | question.

minister [the 2, prime 1, acknowledged 1, question 0]

Context

Word windows (filtered): n words on either side removing some words (e.g. function words, some very frequent content words). Stop-list or by POS-tag.
Example: n=2 (5 words window), stop-list:

| The prime **minister** acknowledged the | question.

minister [prime 1, acknowledged 1, question 0]

Context

3 Lexeme window (filtered or unfiltered); as above but using stems.

Example: n=2 (5 words window), stop-list:

| The prime **minister** acknowledged the | question.

minister [prime 1, acknowledge 1, question 0]

Context

4 Syntactic relations (dependencies). Context for a lexical item is the syntactic dependency structure it belongs to. **Example:**

The prime minister acknowledged the question.

minister [prime 1, acknowledge 1]

minister [prime_mod 1, acknowledge_subj 1]

minister [prime 1, acknowledge+question 1]

Context weighting

- 1. **Binary model**: if context *c* co-occurs with word *w*, value of vector \vec{w} for dimension *c* is 1, 0 otherwise.
- 2. **Basic frequency model:** the value of vector \vec{w} for dimension *c* is the number of times that *c* co-occurs with *w*.
- 3. **Characteristic model**: Weights given to the vector components express how *characteristic* a given context is for word *w*.

Characteristic model

- Weights given to the vector components express how characteristic a given context is for word w.
- Pointwise Mutual Information (PMI)

$$PMI(w,c) = \log \frac{P(w,c)}{P(w)P(c)} = \log \frac{P(w)P(c|w)}{P(w)P(c)} = \log \frac{P(c|w)}{P(c)}$$
$$P(c) = \frac{f(c)}{\sum_{k} f(c_{k})}, \quad P(c|w) = \frac{f(w,c)}{f(w)},$$
$$PMI(w,c) = \log \frac{f(w,c)\sum_{k} f(c_{k})}{f(w)f(c)}$$

f(w, c): frequency of word w in context cf(w): frequency of word w in all contexts f(c): frequency of context c

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What semantic space?

- Entire vocabulary.
 - + All information included even rare contexts
 - Inefficient (100,000s dimensions). Noisy (e.g. 002.png/thumb/right/200px/graph). Sparse
- Top n words with highest frequencies.
 - + More efficient (2000-10000 dimensions). Only 'real' words included.
 - May miss out on infrequent but relevant contexts.
- Dimensionality reduction using matrix factorization
 - + Very efficient (200-500 dimensions). Captures generalisations in the data.
 - The resulting matrices are not interpretable.

Word frequency: Zipfian distribution



number of words

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An example noun

Ianguage:

0.54::other+than+English 0.53::English+as 0.52::English+be 0.49::english 0.48::and+literature 0.48::people+speak 0.47::French+be 0.46::Spanish+be 0.46::and+dialects 0.45::grammar+of 0.45::foreign 0.45::germanic 0.44::German+be

0 44 ·· of+instruction 0.44::speaker+of 0.42::pron+speak 0.42::colon+English 0.42::be+English 0.42::language+be 0.42::and+culture 0.41::arabic 0.41 ·· dialects+of 0.40::percent+speak 0.39::spanish 0.39 welsh 0.39::tonal

An example adjective

- academic:
- 0.52::Decathlon 0.51::excellence 0.45::dishonesty 0.45::rigor 0.43::achievement 0.42::discipline 0.40. viceresident+for 0.39::institution 0.39::credentials 0.38::journal 0.37::journal+be 0.37::vocational 0.37::student+achieve 0.36::athletic

0.36::reputation+for 0.35::regalia 0.35::program 0.35::freedom 0.35::student+with 0.35::curriculum 0.34 standard 0.34::at+institution 0.34::career 0.34::Career 0.33::dress 0.33::scholarship 0.33::prepare+student 0.33::qualification

Polysemy

Distribution for *pot*, as obtained from Wikipedia.

0.57::melt 0.44::pron+smoke 0.43::of+gold 0.41::porous 0.40::of+tea 0.39::player+win 0.39::money+in 0.38::of+coffee 0.33::amount+in 0.33::ceramic 0.33::hot 0.32::boil 0.31::bowl+and 0.31::ingredient+in 0.30::plant+in 0.30::simmer 0.29::pot+and 0.28::bottom+of 0.28::of+flower 0.28::of+water 0.28::of+water

Calculating similarity in a distributional space

Distributions are vectors, so distance can be calculated.



Measuring similarity

► Cosine:

$$\cos(\theta) = \frac{\sum v \mathbf{1}_k * v \mathbf{2}_k}{\sqrt{\sum v \mathbf{1}_k^2} * \sqrt{\sum v \mathbf{2}_k^2}}$$
(1)

- The cosine measure calculates the angle between two vectors and is therefore length-independent.
- Other measures include Euclidean distance etc.

The scale of similarity: some examples

house – building 0.43 gem – jewel 0.31 capitalism – communism 0.29 motorcycle - bike 0.29 test – exam 0.27 school – student 0.25 singer - academic 0.17 horse – farm 0.13 man -accident 0.09 tree – auction 0.02 cat –county 0.007
Words most similar to cat

as chosen from the 5000 most frequent nouns in Wikipedia.

1 cat 0.45 dog 0.36 animal 0.34 rat 0.33 rabbit 0.33 pig 0.31 monkey 0.31 bird 0.30 horse 0.29 mouse 0.29 wolf 0.29 creature 0.29 human 0.29 goat 0.28 snake 0.28 bear 0.28 man 0.28 cow 0.26 fox 0.26 girl 0.26 sheep 0.26 boy 0.26 elephant 0.25 deer

0.25 woman 0.25 fish 0.24 squirrel 0.24 dragon 0.24 frog 0.23 baby 0.23 child 0.23 lion 0.23 person 0.23 pet 0.23 lizard 0.23 chicken 0.22 monster 0.22 people 0.22 tiger 0.22 mammal 0.21 bat 0.21 duck 0.21 cattle 0.21 dinosaur 0.21 character 0.21 kid 0.21 turtle 0.20 robot

But what is similarity?

- In distributional semantics, very broad notion: synonyms, near-synonyms, hyponyms, taxonomical siblings, antonyms, etc.
- Correlates with a psychological reality.
- Test via correlation with human judgments on a test set:
 - Miller & Charles (1991)
 - WordSim
 - MEN
 - SimLex
- Correlation of 0.8 or more.

Distributional methods are a usage representation

- Distributions are a good conceptual representation if you believe that 'the meaning of a word is given by its usage'.
- Corpus-dependent, culture-dependent, register-dependent.
 Example: similarity between *policeman* and *cop*: 0.23

Distribution for policeman

policeman

0.59::ball+poss 0.48. and+civilian 0.42::soldier+and 0.41::and+soldier 0.38::secret 0.37::people+include 0.37::corrupt 0.36. uniformed 0.35::uniform+poss 0.35::civilian+and 0.31::iragi 0.31::lot+poss 0.31::chechen 0.30::laugh 0.29::and+criminal

0.28::incompetent 0.28::pron+shoot 0.28::hat+poss 0.28::terrorist+and 0.27::and+crowd 0.27::military 0.27::helmet+poss 0 27. father+be 0.26::on+dutv 0.25::salary+poss 0.25. on+horseback 0.25::armed 0.24::and+nurse 0.24::job+as 0.24::open+fire

Distribution for *cop*

сор

0.45::crooked 0.45::corrupt 0 44··maniac 0.38::dirty 0.37::honest 0.36::uniformed 0.35::tough 0.33::pron+call 0.32::funky 0.32::bad 0.29::veteran 0.29::and+robot 0.28::and+criminal 0.28::bogus 0.28::talk+to+pron

0.27::investigate+murder 0.26. on+force 0.25::parody+of 0.25::Mason+and 0.25::pron+kill 0.25::racist 0.24::addicted 0.23::gritty 0.23::and+interference 0.23::arrive 0.23::and+detective 0.22::look+way 0.22::dead 0.22::pron+stab 0.21::pron+evade

Clustering nouns



Clustering nouns



Natural Language Processing 1

Semantics with dense vectors

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Semantics with dense vectors

Distributional semantic models

- 1. Count-based models:
 - Explicit vectors: dimensions are elements in the context
 - Iong sparse vectors with interpretable dimensions
- 2. Prediction-based models:
 - Train a model to predict plausible contexts for a word
 - learn word representations in the process
 - short dense vectors with latent dimensions

Sparse vs. dense vectors

Why dense vectors?

- easier to use as features in machine learning (less weights to tune)
- may generalize better than storing explicit counts
- may do better at capturing synonymy:
 - e.g. car and automobile are distinct dimensions in count-based models
 - will not capture similarity between a word with car as a neighbour and a word with automobile as a neighbour

Prediction-based distributional models

Mikolov et. al. 2013. *Efficient Estimation of Word Representations in Vector Space*.

word2vec: Skip-gram model

- inspired by work on neural language models
- train a neural network to predict neighboring words
- learn dense embeddings for the words in the training corpus in the process

Skip-gram



Slide credit: Tomas Mikolov

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Skip-gram

Intuition: words with similar meanings often occur near each other in texts

Given a word w(t):

- Predict each neighbouring word
 - in a context window of 2L words
 - from the current word.
- For L = 2, we predict its 4 neighbouring words:

$$[w(t-2), w(t-1), w(t+1), w(t+2)]$$

Skip-gram: Parameter matrices

Learn 2 embeddings for each word $w_i \in V_w$:

- word embedding v, in word matrix W
- context embedding c, in context matrix C



Skip-gram: Setup

- Walk through the corpus pointing at word w(t), whose index in the vocabulary is j — we will call it w_i
- ► our goal is to predict w(t + 1), whose index in the vocabulary is k we will call it w_k
- to do this, we need to compute

$p(w_k|w_j)$

Intuition behind skip-gram: to compute this probability we need to compute similarity between w_i and w_k

Skip-gram: Computing similarity

Similarity as dot-product between the target vector and context vector



Slide credit: Dan Jurafsky

Skip-gram: Similarity as dot product

Remember cosine similarity?

$$cos(v1, v2) = \frac{\sum v1_k * v2_k}{\sqrt{\sum v1_k^2} * \sqrt{\sum v2_k^2}} = \frac{v1 \cdot v2}{||v1||||v2||}$$

It's just a normalised dot product.

Skip-gram: Similar vectors have a high dot product

 $Similarity(c_k, v_j) \propto c_k \cdot v_j$

Skip-gram: Compute probabilities

Compute similarity as a dot product

$$Similarity(c_k, v_j) \propto c_k \cdot v_j$$

- Normalise to turn this into a probability
- by passing through a softmax function:

$$oldsymbol{arphi}(oldsymbol{w}_k|oldsymbol{w}_j) = rac{oldsymbol{e}^{oldsymbol{c}_k\cdotoldsymbol{v}_j}}{\sum_{i\in V}oldsymbol{e}^{oldsymbol{c}_i\cdotoldsymbol{v}_j}}$$

Skip-gram: Learning

- Start with some initial embeddings (usually random)
- At training time, walk through the corpus
- iteratively make the embeddings for each word
 - more like the embeddings of its neighbors
 - less like the embeddings of other words.

Skip-gram: Objective

Learn parameters C and W that maximize the overall corpus probability:

$$\arg \max \prod_{(w_j, w_k) \in D} p(w_k | w_j)$$

$$p(w_k | w_j) = \frac{e^{c_k \cdot v_j}}{\sum_{i \in V} e^{c_i \cdot v_j}}$$

$$\arg \max \prod_{(w_j, w_k) \in D} p(w_k | w_j) = \prod_{(w_j, w_k) \in D} \frac{e^{c_k \cdot v_j}}{\sum_{i \in V} e^{c_i \cdot v_j}}$$

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Visualising skip-gram as a network



Slide credit: Dan Jurafsky

One hot vectors

- A vector of length |V|
- 1 for the target word and 0 for other words
- So if "bear" is vocabulary word 5
- The one-hot vector is [0,0,0,0,1,0,0,0,0,.....0]

Visualising skip-gram as a network



Slide credit: Dan Jurafsky

Skip-gram with negative sampling

Problem with softmax: expensive to compute the denominator for the whole vocabulary

$$\mathcal{D}(\mathbf{w}_k | \mathbf{w}_j) = rac{\mathbf{e}^{\mathbf{c}_k \cdot \mathbf{v}_j}}{\sum_{i \in V} \mathbf{e}^{\mathbf{c}_i \cdot \mathbf{v}_j}}$$

Approximate the denominator: negative sampling

- At training time, walk through the corpus
- for each target word and positive context
- ▶ sample *k* noise samples or negative samples, i.e. other words

Skip-gram with negative sampling

Objective in training:

 Make the word like the context words lemon, a [tablespoon of apricot preserves or] jam.

 C_1 C_2 W C_3 C_4

And not like the k negative examples

[cement idle dear coaxial apricot attendant whence forever puddle]

 n_1 n_2 n_3 n_4 W n_5 n_6 n_7 n_8

Skip-gram with negative sampling: Training examples

Convert the dataset into word pairs:

Positive (+)

(apricot, tablespoon) (apricot, of) (apricot, jam) (apricot, or)

Negative (-)

```
(apricot, cement)
(apricot, idle)
(apricot, attendant)
(apricot, dear)
```

Skip-gram with negative sampling

- instead of treating it as a multi-class problem (and returning a probability distribution over the whole vocabulary)
- return a probability that word w_k is a valid context for word w_i

$$egin{aligned} & P(+|w_j,w_k) \ & P(-|w_j,w_k) = 1 - P(+|w_j,w_k) \end{aligned}$$

Skip-gram with negative sampling

model similarity as dot product

 $Similarity(c_k, v_j) \propto c_k \cdot v_j$

turn this into a probability using the sigmoid function:

$$\sigma(\mathbf{x}) = \frac{1}{1 + e^{-\mathbf{x}}}$$

$$P(+|w_j, w_k) = \frac{1}{1 + e^{-c_k \cdot v_j}}$$

$$P(-|w_j, w_k) = 1 - P(+|w_j, w_k) = 1 - \frac{1}{1 + e^{-c_k \cdot v_j}} = \frac{1}{1 + e^{c_k \cdot v_j}}$$

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Skip-gram with negative sampling: Objective

- make the word like the context words
- and not like the negative examples

$$\arg \max \prod_{(w_j, w_k) \in D_+} p(+|w_k, w_j) \prod_{(w_j, w_k) \in D_-} p(-|w_k, w_j)$$

 $\arg \max \sum_{(w_j, w_k) \in D_+} \log p(+|w_k, w_j) + \sum_{(w_j, w_k) \in D_-} \log p(-|w_k, w_j) =$

$$\arg\max\sum_{(w_j,w_k)\in D_+}\log\frac{1}{1+e^{-c_k\cdot v_j}}+\sum_{(w_j,w_k)\in D_-}\log\frac{1}{1+e^{c_k\cdot v_j}}$$

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Properties of embeddings

They capture similarity

FRANCE	JESUS	XBOX	REDDISH	SCRATCHED	MEGABITS
454	1973	6909	11724	29869	87025
AUSTRIA	GOD	AMIGA	GREENISH	NAILED	OCTETS
BELGIUM	SATI	PLAYSTATION	BLUISH	SMASHED	MB/S
GERMANY	CHRIST	MSX	PINKISH	PUNCHED	BIT/S
ITALY	SATAN	IPOD	PURPLISH	POPPED	BAUD
GREECE	KALI	SEGA	BROWNISH	CRIMPED	CARATS
SWEDEN	INDRA	PSNUMBER	GREYISH	SCRAPED	KBIT/S
NORWAY	VISHNU	HD	GRAYISH	SCREWED	MEGAHERTZ
EUROPE	ANANDA	DREAMCAST	WHITISH	SECTIONED	MEGAPIXELS
HUNGARY	PARVATI	GEFORCE	SILVERY	SLASHED	GBIT/S
SWITZERLAND	GRACE	CAPCOM	YELLOWISH	RIPPED	AMPERES

Slide credit: Ronan Collobert

Properties of embeddings

They capture analogy

Analogy task: a is to b as c is to d

The system is given words *a*, *b*, *c*, and it needs to find *d*.

"apple" is to "apples" as "car" is to ? "man" is to "woman" as "king" is to ?

Solution: capture analogy via vector offsets

$$a-b \approx c-d$$

$$man - woman \approx king - queen$$

 $d_w = \operatorname*{argmax}_{d' \in V} cos(a - b, c - d')$

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(日)

Properties of embeddings

Capture analogy via vector offsets





Mikolov et al. 2013. *Linguistic Regularities in Continuous Space Word Representations*
-Semantics with dense vectors

Properties of embeddings

They capture a range of semantic relations

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

Mikolov et al. 2013. *Efficient Estimation of Word Representations in Vector Space*

- Semantics with dense vectors

Word embeddings in practice

Word2vec is often used for pretraining in other tasks.

- It will help your models start from an informed position
- Requires only plain text which we have a lot of
- Is very fast and easy to use
- Already pretrained vectors also available (trained on 100B words)

However, for best performance it is important to continue training, fine-tuning the embeddings for a specific task.

-Semantics with dense vectors

Count-based models vs. skip-gram word embeddings

Baroni et. al. 2014. Don't count, predict! A systematic comparison of context-counting vs. context-predicting semantic vectors.

- Comparison of count-based and neural word vectors on 5 types of tasks and 14 different datasets:
 - 1. Semantic relatedness
 - 2. Synonym detection
 - 3. Concept categorization
 - 4. Selectional preferences
 - 5. Analogy recovery

-Semantics with dense vectors

Count-based models vs. skip-gram word embeddings



Some of these findings were later disputed by Levy et. al. 2015. *Improving Distributional Similarity with Lessons Learned from Word Embeddings*

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Semantics with dense vectors

Acknowledgement

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